TOWARDS IMPROVING RATE-DISTORTION PERFORMANCE OF TRANSFORM-BASED LOSSY COMPRESSION FOR HPC DATASETS

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OUTLINE

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- ENERGY COMPACTION BASED COMPRESSION ALGORITHM
- EXPERIMENT EVALUATION
- CONCLUSION



INTRODUCTION

SCIENTIFIC SIMULATION FRAMEWORKS (HPC SIMULATIONS)

• High-performance computing (HPC)

- Perform research activities through computer modeling, simulation, and analysis.
- Large volumes of data, reaches exabyte range
 - Periodic checkpointing (checkpoint/restart)
 - Post-simulation data analysis
- File systems in extreme-scale systems
 - Limited storage space and I/O time, e.g.:
 - 170 TB of CESM data is being produced by CMIP5 project
 - n*PB data will be generated for upcoming CMIP6 experiments per entire run
 - Yellowstone (supercomputer): tens of PB of centralized file system and data storage





INTRODUCTION

DATA REDUCTION/DATA COMPRESSION

- Data Reduction/Data Compression
 - Lossless Compression: 100% of data fidelity (fully invertible, 1:1 copy), but not able to achieve appreciable data reduction (GZIP, BZIP, etc.)
 - Lossy Compression: high compression ratio, but error introduced (SZ, ZFP, etc.)

- Floating Point Data Compression (Scientific Simulations)
 - e.g., double precision
 - High precision on reconstructed (decompressed) data
 - Randomness



INTRODUCTION

LOSSY COMPRESSION TECHNIQUES FOR SCIENTIFIC DATA

• Understanding Errors

- Scientific data can tolerate a certain amount of accuracy loss
- Errors are inherent in scientific simulations (generated from inaccurate scientific sensors)
- Study by Tao et al.: A comprehensive study of lossy compression on HPC datasets
 - Examined the impact of reduced accuracy on scientific data analysis frameworks.
 - In-depth understanding of the benefits and pitfalls (lossy compression)



ANALYSIS OF TRANSFORM-BASED LOSSY COMPRESSION

TRANSFORM-BASED LOSSY COMPRESSION

- Discrete Data Transform (DCT, HWT, CDF 9/7, etc.)
- Decorrelation (vs. time domain)
- Energy Compaction Property
 - Energy of a signal

$$\varepsilon_{f=} \sum_{n=1}^{N} |f_n|^2, n = 1, 2, \dots, N,$$

- Energy Compaction Rate (ECR)

$$ECR_f = \frac{\sum_{n=1}^{M} |f_n|^2}{\sum_{n=1}^{N} |f_n|^2}, n = 1, 2, \dots, N, M \le N.$$



ANALYSIS OF TRANSFORM-BASED LOSSY COMPRESSION

• Estimation of Energy Compaction on Various Transform

Real-world HPC datasets

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| Transform | Threshold | rlds | mrsos | sedov | cellular | Eddy | Vortex |
|-----------------------------|-----------|-------|-------|-------|----------|-------|--------|
| Original | 1/32 | 6.03 | 21.65 | 27.27 | 6.53 | 25.91 | 44.28 |
| | 1/64 | 3.09 | 11.63 | 15.50 | 3.45 | 16.08 | 28.12 |
| | 1/32 | 99.81 | 91.36 | 94.50 | 99.49 | 94.78 | 98.35 |
| DC I-II | 1/64 | 99.69 | 88.17 | 92.06 | 99.13 | 89.29 | 96.93 |
| HWT 5-level | 1/32 | 96.94 | 33.22 | 65.91 | 92.86 | 36.64 | 36.01 |
| HWT 6-level | 1/64 | 93.63 | 17.60 | 47.87 | 86.67 | 18.12 | 20.19 |
| CDF 9/7 5-level | 1/32 | 98.08 | 39.17 | 62.78 | 91.82 | 24.76 | 27.07 |
| CDF 9/7 6-level | 1/64 | 95.83 | 21.58 | 44.46 | 84.47 | 11.97 | 15.47 |
| DCT HWT-2 HWT-6 CDF-2 CDF-6 | | | | | | | |
| 0% | 2% | | 4% | 6% | | 8% | |
| Total coefficient used | | | | | | | |

ENERGY COMPACTION BASED COMPRESSION ALGORITHM

DCT (DISCRETE COSINE TRANSFORM)- BASED LOSSY COMPRESSION

- Block Decomposition with DCT
- Energy Compaction based compression algorithm
 - Compression with a fixed energy compaction rate (*ECR*)
 - Compression with an optimal energy compaction rate (*ECR*)



COMPRESSION WITH A FIXED ENERGY COMPACTION RATE

- Fixed Energy Compaction Rate (ECR)
- Find top dominant block coefficients



COMPRESSION WITH AN OPTIMAL ENERGY COMPACTION RATE

• Spline Fitting Kneedle Algorithm - Knee-point $K_f(x) = \frac{f''(x)}{(1 + f'(x)^2)^{1.5}},$ 0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8 0.9 1.0 0.0 Normalized Number of Coefficients



COMPRESSION WITH AN OPTIMAL ENERGY COMPACTION RATE

Spline Fitting

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- 1D interpolation
- Polynomial interpolation





APPROXIMATION & ENCODING

> Adjustable error-controlled quantizer

- Equal width binning
- Approximate as bin's center value
- Fixed error bound

Encoding

- Dominant coefficient
- Approximation: bin center values
- Bin indices (and QT)
- Lossless add-on





EVALUATION (EXPERIMENTAL SETUP & APPLICATIONS)

- Conduct on Massachusetts Green High Performance Computing Cluster (MGHPCC)
- 6 real-world scientific datasets
 - rlds, mrsos, cellular, sedov, vortex, eddy

| Code | Description |
|---------|--|
| FLASH | Physics Solvers implicit with AMR |
| CMIP5 | Coupled Model Intercomparison Project World Climate |
| Nek5000 | High-order Solver for fluid dynamics |

| Code | Dataset | Value Range | Avg Value | Entropy | Dimension |
|--------------|----------|---------------|----------------|---------|-----------|
| FLASH [21] | sedov | 4.2385 | 1.0000 | 4.9702 | 31040*154 |
| | cellular | $2.6482E^{7}$ | $2.2083E^{7}$ | 4.1190 | 32768*295 |
| CMIP5 [22] | rlds | 361.2303 | 285.8844 | 7.2106 | 12960*100 |
| | mrsos | 44.5000 | 7.6916 | 4.4864 | 12960*100 |
| Nek5000 [23] | eddy | 4.8345 | $3.2366E^{-8}$ | 7.6047 | 16384*999 |
| | vortex | 0.0550 | 0.0017 | 7.5797 | 37024*99 |













EVALUATION (SCHEMES & METRICS)

- Evaluation Schemes
 - A1: compression with fixed energy compaction rate.
 - A2: compression with optimal energy compaction rate.
 - A2_interp1d: A2 using 1D interpolation.
 - A2_polynomial: A2 using polynomial interpolation.
 - A1_B: A1 with equal-width-binning.
 - A2_interp1d_B & A2_polynomial_B: A2_interp1d and A2_polynomial with equal-width-binning, respectively.

- Rate-Distortion
 - Bit-rate (smaller bit-rate represents higher compression ratio)
 - Distortion: PSNR (higher
 PSNR represents less error)



EVALUATION

COMPARISON BETWEEN FIXED AND OPTIMAL ENERGY COMPACTION RATES



- A1→A1_B PSNR↑ 15.8dB
- A2_interp1d_B→A1_B PSNR ↑2.46dB (mrsos, 6.49dB)
- 5.5 bit (~99% Energy)
- 6.67 bit (~97% Energy)



EVALUATION

RATE-DISTORTION AND BLOCK SIZE



EVALUATION

SPLINE FITTING

Total number of coefficients (on average) used in each block

| Algorithm | sedov | cellular | rlds | mrsos | eddy | vortex |
|------------|-------|----------|-------|--------|-------|--------|
| Interp1d | 3.929 | 6.844 | 9.356 | 11.172 | 9.597 | 11.925 |
| Polynomial | 3.853 | 6.449 | 9.557 | 10.956 | 9.182 | 10.122 |

Average energy compaction rate (%)

| Algorithm | sedov | cellular | rlds | mrsos | eddy | vortex |
|------------|-------|----------|-------|-------|-------|--------|
| Interp1d | 98.44 | 99.59 | 99.99 | 99.99 | 89.83 | 93.55 |
| Polynomial | 98.44 | 99.59 | 99.99 | 99.99 | 90.12 | 91.08 |



CONCLUSION

- We analyze different transforms by exploiting their energy compaction property. By finding an optimal energy compaction rate based on our knee detection algorithm, our compression technique can acquire the best trade-off solution between information loss and compression rate.
- Specially, on average, only 6.67 bits are required to preserve an optimal energy compaction rate on our evaluated datasets. Our knee detection algorithm improves the distortion in terms of peak signal-to-noise ratio by 2.46 dB on average.



THANK YOU

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Learning with Purpose